

## LEVEL 4 MATHEMATICS REVISION OF NUMBER

## Numbers in everyday life

- Paying bills • Sport
- Shopping
- Selling
- Cooking
- Travelling
- Measuring • Budgeting
- Medication
- Salaries
- Benefits
- Science
- Statistics
- Computers


## Resetting your calculator

- Shift 9
- Choose 3 (All)
- Choose = (Yes)
- Choose AC (Reset all)



## Setting up your calculator for Assignment 1

- Shift
- Mode set-up
- Press 2 (Linear)



## Converting currencies

- To change Irish money to foreign money multiply by the exchange rate.
- To change foreign money to euro - divide by the exchange rate.

$$
\text { E.g. 1.00 EUR }=\quad \text { 1.29573 USD }
$$

$$
\begin{aligned}
€ 45 & =1.29573 \times 45=\$ 58.31 \\
\$ 45 & =45 \div 1.29573=€ 34.73
\end{aligned}
$$

## Converting fractions, decimals, \%

## Percent Conversions - Summary



## Converting fractions, decimals, \%

- Examples:

| Fraction | Decimal | Percentage |
| :--- | :--- | :--- |
|  | Divide top number <br> (numerator) by <br> bottom number <br> (denominator) | $\times 100$ |
| $1 / 2$ | 0.5 | $50 \%$ |
| $1 / 4$ | 0.25 | $25 \%$ |
| $3 / 4$ | 0.75 | $75 \%$ |

## Ratios

- If there are 4 men and 8 women (lucky men!), the ratio will be:
4: 8
- This can be simplified as 4 will divide into each:
1: 2


## Conversions....

- Example:

| Fraction | Decimal | Percent (\%) | Ratio |
| :---: | :---: | :---: | :---: |
| $\frac{1}{4}$ | 0.25 | 25 | $1: 4$ |
| $\frac{3}{8}$ | 0.375 | 37.5 | $3: 8$ |
| $\frac{5}{6}$ | $0.83 \overline{3}$ | $83 . \overline{3}$ | $5: 6$ |

## Standard form to scientific notation

$$
51,300
$$

Write this number using scientific notation. Use ' $x$ ' for multiplication.

$$
5.13 \times 10^{4}
$$

## Scientific notation on your calculator

To convert from standard form to scientific notation on your calculator:

- Shift
- Mode Set-up
- Choose 7 (scientific)
*Don't forget to reset your calculator when you are done!!!!

Scientific notation to standard form Positive Power = Large Number
$\mathbf{4 . 3 \times 1 0 ^ { 6 } = 4 3 0 0 0 0 0}$

Negative Power = Small Number $2.1 \times 10^{-3}=0.021$

## Significant figures



## Approximation

- This is when you work out the answer by approximating, for example, by rounding numbers.

Example: $192+2349$ : You might round these to 200 and 2300 and your approximate answer might be 2500.

## Percentage error

## |Approximate Value - Exact Value|

|Exact Value|

Number sets

Rational Numbers
Includes the other 3 sets plus repeating and terminating decimals and fractions $-0.3, \frac{2}{3},-\frac{5}{2}, 0.6666$ and their opposites.

Integers
Includes all the Whole numbers and their opposites. Positive and negatives, $-3,-2,-1,0,1,2,3$

Natural or Counting Numbers
Whole Numbers
These numbers can be shown with objects.
Include the natural numbers They begin with $1,2,3$, and continue forever. plus zero. $0,1,2,3 \ldots$

Irrational Numbers
These numbers are represented by non-repeating, non-terminating decimals and their opposites.
Examples: $\pi, \quad \sqrt{3}, \sqrt[3]{5},-\sqrt{5}$

## Laws of indices

### 5.1 INDICES AND LAWS OF INDICES

1. $a^{n}, a$ is a base and $n$ is an index
2. The laws of indices are:
(i) $a^{m} \times a^{n}=a^{m+n}$
(ii) $a^{m} \div a^{n}=a^{m-n}$
(iii) $\left(a^{m}\right)^{n}=a^{m n}$
(iv) $(a b)^{n}=a^{n} b^{n}$
$(\mathrm{v})\left(\frac{a}{b}\right)^{n}=\frac{a^{n}}{b^{n}}$

## Rules of logarithms

## Simplify expressions

- Find all the like terms.
- Example:
- $6 \boldsymbol{x}-x y+5 x-7 x y$
$=6 x+5 x=11 x$ and $-x y-7 x y=-8 x y$
$=11 x-8 x y$


## Simplifying expressions

- Example: multiply everything in the brackets by the number in front:
- $3(2 x-y+4)+2(x+y-3)$

$$
=6 x-3 y+12+2 x+2 y-6
$$

- Find the like terms

$$
=8 x-y+6
$$

## Solving equations

- Try to get the unknown, e.g. $x$, onto the left hand side
- Example:
- $3 x-8=13$

To move the 8 over to the other side, change the operation

- $3 x=13+8$
- $3 x=21$
- $x=21 \div 3$
- $x=7$


## Simple and compound interest

Vocabulary:

- $P=$ Principal
- $r=$ Rate of interest (divide this by 100)
- t = time


## Simple interest

- I = prt
- (Interest $=$ principal $\times$ rate $(\div 100) \times$ time (years)

Example: If I save $€ 1,200$ at a rate of $3 \%$ for 4 years, how much do I have at the end of the 4 years?
I = prt
I $=1,200 \times(3 \div 100) \times 4$
$\mathrm{I}=144$
I saved $€ 1,200$ and the interest is $€ 144$ so I must add the two!
$1,200+144=€ 1,344$ Total amount

# Compound interest 

Use this formula:

$$
A=P\left(1+\frac{r}{\mathbf{1 0 0}}\right)^{n}
$$

## Example of compound interest

- Principal $=€ 5500$, Rate $=4.3 \%$, Number of years $=6$
- $A=P\left(1+\frac{r}{100}\right)^{n}$
- $A=5500\left(1+\frac{4.3}{100}\right)^{6}$ (Work out your interest first)
- Type into your calculator:
- $5500(1+0.043)^{6}$ (Use $x$ to the little box, and type in 6)
- $=€ 7080.58$


## Income

## Vocabulary:

- Gross salary - overall salary
- Net salary - Gross salary - reductions
- PRSI - Pay Related Social Insurance
- Tax - must be deducted from the gross
- Tax credits - must be deducted from total tax
- Remember to subtract all the deductions from the gross salary.

Helen earns $€ 368.00$ per week. Her deductions are: $20 \%$ tax, $2 \%$ PRSI, $€ 32$ tax credits. What is her net salary per week:
$368 \times 20 \%$ tax $=€ 73.60$
$73.60-32$ (tax credits) $=€ 41.60$
$368 \times 2 \%($ PRSI $)=€ 7.36$
Gross salary - Tax - PRSI $=$ Net Pay
$368-41.60-7.36$
= €319.04 Net Salary

## Profit

- Profit = selling price - cost price

Example: If I buy 10 televisions for $€ 5,000$ and I sell them for $€ 690$ each, how much profit do I make if I sell all of them?

Cost to me: $5,000 \div 10=€ 500$. I paid $€ 500$ for each TV.
If I sell them @ €690 each: $690 \times 10=€ 6,900$. I made $€ 6,900$.
I paid $€ 5,000$ and I sold them for $€ 6,900$ so the amount of profit $=6,900-5,000=€ 1,900$ Profit.

Percentage profit $=$ Profit that I made $\div$ Price that I paid $\times 100$ $1,900 \div 5,000 \times 100=38 \%$ Profit

## LOSS

## - Profit = cost price - selling price

Example: If I buy 10 televisions for $€ 5,000$ and I sell them for $€ 450$ each, what is my loss if I sell all of them?

Cost to me: $5,000 \div 10=€ 500$. I paid $€ 500$ for each TV.
If I sell them @ €450 each: $450 \times 10=€ 4,500$. I made $€ 4,500$.
I paid $€ 5,000$ and I sold them for $€ 4,500$ so the amount of loss $=5,000-4,500=€ 500$ Loss.
Percentage loss $=$ The loss $\div$ cost price $\times 100$
$500 \div 5,000 \times 100=10 \%$ Loss

## VAT

- VAT stands for Value Added Tax.
- Value Added Tax (VAT) is a tax charged on the sale of goods or services and is included in the price of most products and services that we use every day.

Example:

$192.76 \times 13.5$ (shift) \%

- Total due
€218.78
= 26.02
Don't forget - you must add
Pay by
Direct Debit
your VAT to the total!!!

= €218.78 Total Bill

